

### LEAP The Planetary Boundary Layer



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## The Planetary Boundary Layer (PBL)

- Lowest layer of troposphere (~1 km)
  - Events are often too small to be resolved by climate models (~100km)
  - Directly affected by surface heating/cooling
  - Turbulent, well-mixed, unstable
  - Capped by a temperature "inversion"
- Vertical turbulent fluxes
  - $\circ \quad \text{Surface heat} \rightarrow \text{buoyancy}$
  - Transport air and key quantities upward:
    - Pollution, heat, moisture, etc...







### The Data

- Simulate PBL using Large Eddy Simulations (LES)
- Varying initial conditions: horizontal wind, surface heating, inversion strength
- Captures evolution of PBL at high resolution (24×24×6 m, 120 min)
- Coarse-grained and averaged down to vertical profile to remove noise
- Many variables and their higher order moments produced.



2D Slice of Vertical Velocity in PBL Simulation



# Symbolic Regression (SR)

A machine learning task which aims to discover human-interpretable equations.

- Genetic algorithm + optimization task
- Combines operators (+,-,×,÷), basic functions (sin, cos, inv), and coefficients.
- Inputs: response variable, potential predictor variable(s)
- Output: Equation relating predictors and response
- Inherently very random, not guaranteed to converge or find correct equation







# **Eq 1: Entrainment Velocity**

- How does the PBL grow over time?
- At the capping inversion:
  - Inertia of rising air overshoots to the free troposphere
  - This causes mixing at the PBL
- Represented by  $rac{dh}{dt}$  or  $w_e$ 
  - Large scale components in  $\frac{dh}{dt}$  are not considered in our LES



Horizontal distance, x

[4]



# Eq 1: Discovering entrainment velocity

• Current parameterization:

$$\frac{dh}{dt} = A \frac{\overline{w'b'}_{\text{sfc}}}{\frac{g}{\theta_0} \Delta \theta_{\rho}}$$

• Discovered equation:

$$\frac{dh}{dt} = -10.751 \frac{\overline{w'b'}_{\rm sfc}}{\Delta\theta_{\rho}} - 0.00076 U_g$$





# **Eq 2: Inversion Layer Mass-Flux**

- Calculation discrepancies • Some textbooks [7] say:  $h^{-} \frac{d\theta_{ml}}{dt} = \overline{w\theta_{h^{-}}} + \overline{w\theta_{sfc}}$ 
  - Where:  $\overline{w\theta_{h^-}} = w_e \Delta \theta_{
    ho}$
- Looking for the mass flux in the inversion layer
  - Equation discovery struggles to adhere to physics & respect units





### Eq 3: Heat Flux

We model the way the turbulent component of warm air vertically transports key quantities in the PBL ( $\overline{w\theta}$ ) First, the pressure redistribution term is found, as derived in [6]:

$$P = -\frac{1}{\rho_0} \overline{\theta \frac{\mathrm{d}p}{\mathrm{d}z}} = -C_1 \frac{\overline{w\theta}}{\tau_1} - C_2 \beta \overline{\theta^2} + C_3 \sigma_w^2 \frac{\mathrm{d}\Theta}{\mathrm{d}z}$$

Then, the resulting coefficients  $C_1, C_2, C_3$  are plugged into a parametrization for  $\overline{w\theta}$  that is dependent on them.

#### Goals:

- 1. Verify the functional form for *P*, using the above predictors and response
- 2. If correct, compare discovered coefficients to theoretical/typical estimates
- 3. Plug coefficients in to test to see how well  $\overline{w\theta}$  is parametrized.



# Eq 3: Goals 1 & 2

• Rediscovery of eq for *P* is successful after lots of tuning: functional form appears correct





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# Eq 3: Goals 1 & 2

- Rediscovery of eq for P is successful after lots of tuning: functional form appears correct
- Final eq provides excellent fit.
- Coefficients differ strongly from theoretical/typical values







When coefficients are plugged back into  $\overline{w\theta}$  parametrization, performance is bad..

- Discrepancy most likely from data issues, or extra dependency on large scale forcings.
- A second stage SR on the coefficients shows that  $C_1$  may be dependent on  $U_g$ .
- This makes sense: horizontal wind likely speeds up mixing.





## Conclusions

#### **Our Contributions:**

- Equation rediscovery: w<sub>e</sub>, P
- Equation improvement: better coefficients & dependencies on large scale forcings
- Attention drawn to horizontal wind
- Github repo for reproducibility + future work

#### **Future Directions:**

- Include more simulations with varying initial conditions
- Refine the second stage SR for finding coefficient dependence on large scale forcings
- Building in physics/consideration of units
- One big limitation of equation discovery is reliance on local information, bring in non-locality (function space or inputs)



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